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STRAIN BEHAVIOR OF PRESSURIZED CRACKED THICK-WALLED CYLINDERS

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August 1980



US ARMY ARMAMENT RESEARCH AND DEVELOPMENT COMMAND
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AMCMS No. 612105H840011

DA Project No. 1L162105AH84

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ACKNOWLEDGMENTS

We express our appreciation to R. R. Lasselle who conceived the strain monitoring technique, R. T. Abbott for instrumentation and testing, C. A. Monarch for drafting, and C. J. Crell for illustrations. We also dedicate this work to the memory of Mike Lombard whose enthusiasm gave us a good start but who didn't make it all the way.

LIST OF SYMBOLS

a	= crack depth
$a/2c$	= aspect ratio, crack depth to length
$a/(R_2-R_1)$	= ratio of crack depth to wall thickness
D_i	= inside diameter
D_o	= outside diameter
L	= cylinder specimen length
N	= fatigue cycles
N_f	= cycles for failure
P	= internal hydraulic pressure
R	= radius to any point inside cylinder wall
R_a	= radius from center to crack tip
R_1	= inside radius
R_2	= outside radius
t	= wall thickness
x	= ratio of cycles at a given crack depth to the cycles for failure
y	= ratio of measured strain in the crack plane to the theoretical Lamé strain on the outside of an uncracked cylinder
$2c$	= longitudinal length of crack
% OS	= percent overstrain
ϵ	= measured circumferential strain
ϵ_o	= measured circumferential strain at crack plane
ϵ_{th}	= theoretical Lamé strain at OD of uncracked cylinder

ϵ_o/ϵ_{th}	= ratio of crack plane strain to Lamé strain
ϕ	= angle from crack plane
σ	= stress
σ_I	= internal stress at crack tip
σ_o	= stress on outside surface
σ_y	= yield stress
σ/P	= ratio of stress to pressure

INTRODUCTION

An experimental method for measuring crack growth of internally cracked thick-walled cylinders under pressure was developed by Lasselle.¹ The strain pattern on the outside surface of the cylinder deviates from the Lamé' strain behavior as the crack grows outward through the cylinder wall. Shannon² has pointed out from the experimental data of Lasselle that the pressure-bending effect on the outside of the cylinder is mainly confined to the surface region between ± 7 degrees of the plane of the radial crack. He concluded that strain measurements will measure crack depth accurately and will detect changes in crack depth with the same sensitivity as a crack-opening-displacement gage when used with high-strength materials. The major advantage of the local-strain-sensing technique is the relative ease with which it can be used for automated monitoring of crack growth.

In order to enhance our understanding of the crack growth behavior of internally pressurized cylinders, we have studied the relationship of the external experimental circumferential strains of the cylinders as functions of pressure, increasing crack depth, crack shape and percent overstrain. The stresses and strains are compared with theoretical Lamé' values for the uncracked specimen. This study is a continuation of the study of cracked

¹Underwood, J. H., Lasselle, R. R., Scanlon, R. D., and Hussain, M. A., "A Compliance K-Calibration for a Pressurized Thick-Walled Cylinder With a Radial Crack," Eng. Fract. Mech., 4, 231-44, (1972).

²Shannon, R. W. E., "Crack Growth Monitoring by Strain Sensing," Pres. Ves. & Piping, (1), pp. 61-73, Appl. Science Publ. Ltd, England (1973).

C-shaped specimens³ reported previously. The results show that suitable choice of gage location and appropriate calibration relationships can enable automatic strain-gage monitoring of crack growth and prediction of failure in thick-walled cylinders.

APPARATUS, INSTRUMENTATION, AND PROCEDURE

The strains on the external surface of 30 inch (0.76 m) long cylinders of high strength steel were measured with bonded foil strain gages while pressurized in steps from zero to 48 ksi (330 MPa). The cylinders were 7.1 inches (180 mm) bore diameter with 14.25 inches (360 mm) outside diameter and were fatigue cracked from longitudinal internal notches. Three initial notch geometries were used; semicircular, 4 inch (100 mm) and 20 inch (500 mm) long notches produced by electrical discharge machining. They were 1/4 inch (6.4 mm) deep by 0.030 inch (0.76 mm) wide, the semicircular notch being 1/2 inch (13 mm) diameter half-penny shape. The external strains on the periphery at mid-section of the cylinder were measured at crack depths 1/4 inch (6.4 mm) to 3 inches (76 mm) measured from the bore, generally at intervals of 1/2 inch (13 mm).

Figure 1 shows a schematic diagram of a typical cylinder with initial notch and the growth of a 20 inch (500 mm) long notch from 1/4 inches (6.4 mm) initial depth by repeated pressurization to 48 ksi (330 MPa).

³Throop, J. F. and Fujczak, R. R., "Stress, Strain and Deflection of Cracked C-Shaped Specimens," Experimental Mechanics, Vol. 17, No. 8, pp. 290-296, (1977).

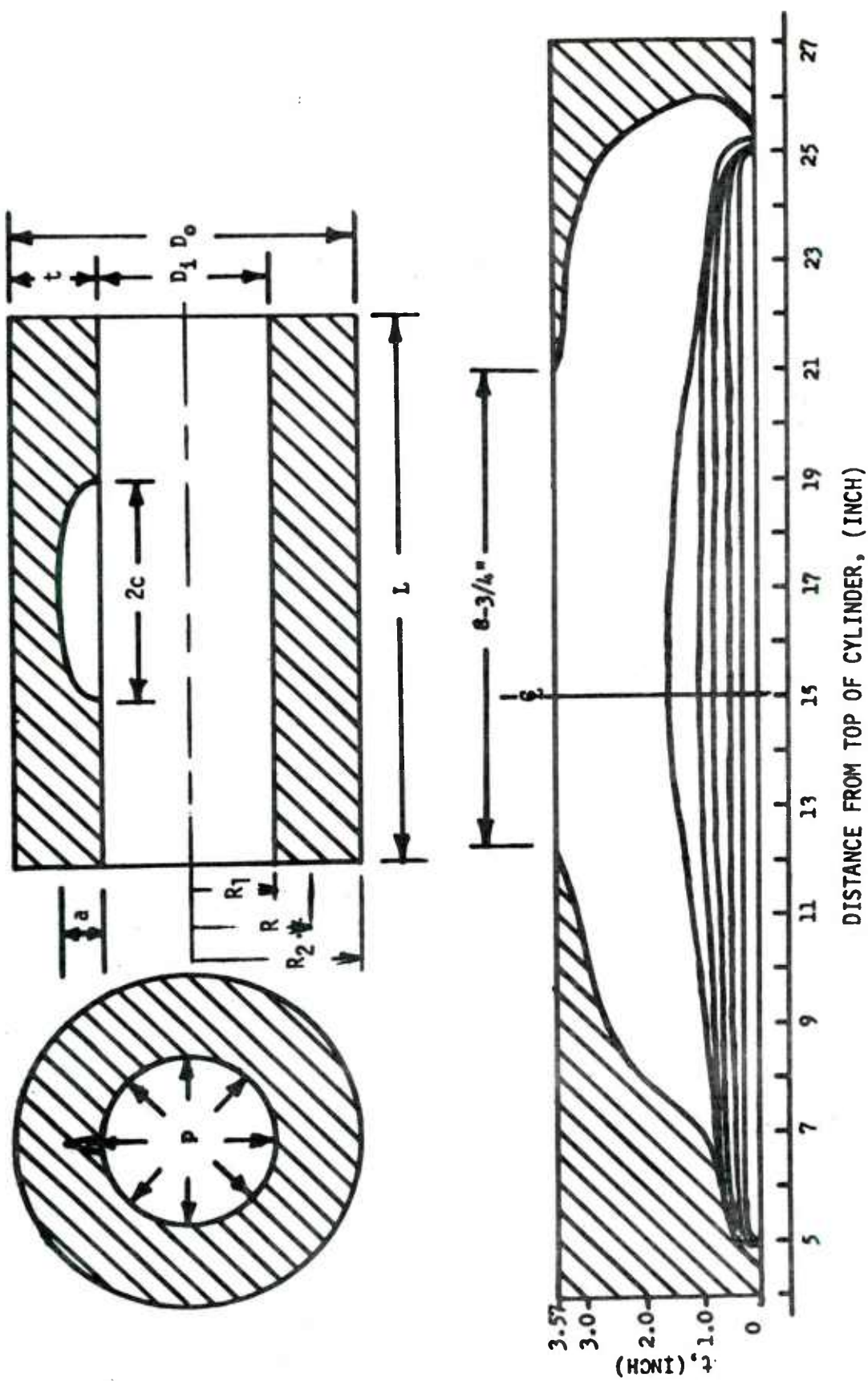


Fig. 1 PRESSURIZED CRACKED CYLINDER

The gages were mounted circumferentially with two directly over the notch line, equally spaced on either side of the cylinder midsection, and at 5°, 15°, 30°, 60°, 90°, 135°, and 180° on either side of the notch. Strain measurements were made on non-autofrettaged cylinders, and on cylinders with 30% overstrain and 60% overstrain produced by hydraulic autofrettage. The percent overstrain is the portion of the wall thickness which has exceeded the material yield strength during the prestressing by overpressurization. Specimens with single notch, two opposing notches and four equally spaced notches were tested. The bore of the cylinder was partially filled with a cylindrical steel mandrel which supported the end closures, leaving the cylinder in essentially the open-end condition. A synthetic hydraulic oil was used as the pressurizing medium, filling the remainder of the cavity including the notch. Fatigue cracks grown from the initial notches were monitored for depth and shape with ultrasonics periodically as the cylinder was repeatedly pressurized from 4 ksi (28 MPa) to 48 ksi (330 MPa). The growth of fatigue cracks in cylinder specimens is described by Throop⁴ and the 175 mm fatigue specimens, end packing, and ultrasonic crack depth measurements are described by Davidson et al.⁵

⁴Throop, J. F., "Fatigue Crack Growth in Thick-Walled Cylinders," Proceedings National Conference on Fluid Power, Vol. XXVI, pp. 115-131, NCFP, Chicago, (1972).

⁵Davidson, T. E., Throop, J. F., and Reiner, A. N., "The Role of Fracture Toughness and Residual Stresses in the Fatigue and Fracture Behavior of Large Thick-Walled Pressure Vessels," Proceedings National Conference on Fluid Power, Vol. XXVI, pp. 102-114, NCFP, Chicago, (1972).

The strain readings were taken under static pressurization using a null-balancing technique, and up to 20 gages were recorded at several pressures to maximum pressure and back to zero again.

STRESS AND STRAIN EQUATIONS

(a) The stress and strain on the outside surface and stress on the inside surface may be calculated by the following equations:⁶

$$\sigma_o = P \frac{2R_1^2}{(R_2^2 - R_1^2)} \quad \text{on outside surface} \quad (1)$$

$$\epsilon_{th} = \frac{P}{E} \frac{2R_1^2}{(R_2^2 - R_1^2)} \quad \text{on outside surface} \quad (2)$$

$$\sigma_i = P \frac{(R_2^2 + R_1^2)}{(R_2^2 - R_1^2)} \quad \text{on inside surface} \quad (3)$$

(b) Cylinder radial displacement may be related to circumferential surface strain by the following equation:

Circumferential surface strain equals cylinder unit radial displacement:

$$\epsilon_{circ} = \frac{2\pi(R + \Delta R) - 2\pi R}{2\pi R} = \frac{\Delta R}{R} \quad (4)$$

So the radial deformation, ΔR , may be calculated by the following equation:

$$\Delta R = R \times \epsilon_{circ} \quad (5)$$

⁶ Timoshenko. S. P. and Goodier, J. N., Theory of Elasticity, Third Edition, McGraw-Hill Book Company, New York, pp. 68-71 (1970).

(c) An idealization presented by Shannon² assumes wall thinning represented by an effective increase of the internal radius of the cylinder to include the crack depth, with the pressure-bending effect applied as a moment on a section of depth equal to the remaining wall thickness of the cylinder. Thus, the equations for stress and strain on the outside surface are as follows.

Uniform-thinning and pressure-bending approximation for stress and strain in cylinder with internal longitudinal straight-fronted crack of depth $a = (R_a - R_1)$; (Shannon, 1973):

Outside Surface:

$$\sigma_o = \frac{2PR_a^2}{(R_2^2 - R_a^2)} - \frac{3P(R_a - R_1)(R_2 - R_1)}{(R_2 - R_a)^2} \quad (6)$$

$$\epsilon_o = \frac{\sigma_o}{E} \quad (7)$$

A similar expression approximating the stress at the inside of the crack is:

$$\sigma_I = P \frac{(R_2^2 + R_a^2)}{(R_2^2 - R_a^2)} + \frac{3P(R_a - R_1)(R_2 - R_1)}{(R_2 - R_a)^2} \quad (8)$$

These equations are plotted in Figure 9 which will be discussed later.

EXPERIMENTAL RESULTS

The approximately 200 strain readings at each crack depth were computer-smoothed with an interpolating spline function to provide a continuous expression of strains around the periphery at the cylinder midsection. The

²Shannon, R. W. E., "Crack Growth Monitoring by Strain Sensing," Pres. Ves. & Piping, (1), pp. 61-73, Appl. Science Publ. Ltd., England (1973).

results were plotted in two forms: (a) strain versus equatorial angle in rectangular coordinates, and (b) circumferential strain plotted as a radial vector in polar coordinates. The latter plot forms an interesting figure which, in the case of a single crack, is heart-shaped with the cusp directly over the crack plane, like a cardioid. This plot is shown in Figure 2. Note that the cusp coincides with the crack plane. For zero crack depth, $a = 0$, the Lamé theoretical strain plots as a circle.

In the case of multiple cracks, as shown in Figure 3, the shape becomes like an epicycloid, where for dual opposing notches (Figure 3a) the two cusps occur directly over the cracks, and for four notches (Figure 3b), there are four cusps directly over the four cracks.

These figures are significant since it is shown by Equations (4) and (5) that the external circumferential strain at a point on a cylinder is equal to the actual unit radial deformation $\Delta R/R$ at that same point. Hence the radial deformation is proportional to the circumferential strain and the shape of the figure is an exaggerated representation of the distorted shape of the cracked pressurized cylinder. When compared with the theoretical Lamé circumferential strain for the given pressure, the figure shows the difference in shape of the cracked cylinder from that of an uncracked cylinder at pressure. The consequent bending of the cylinder wall at the sites of sharp curvature and the sites of cusps in the figure therefore becomes apparent, although exaggerated.

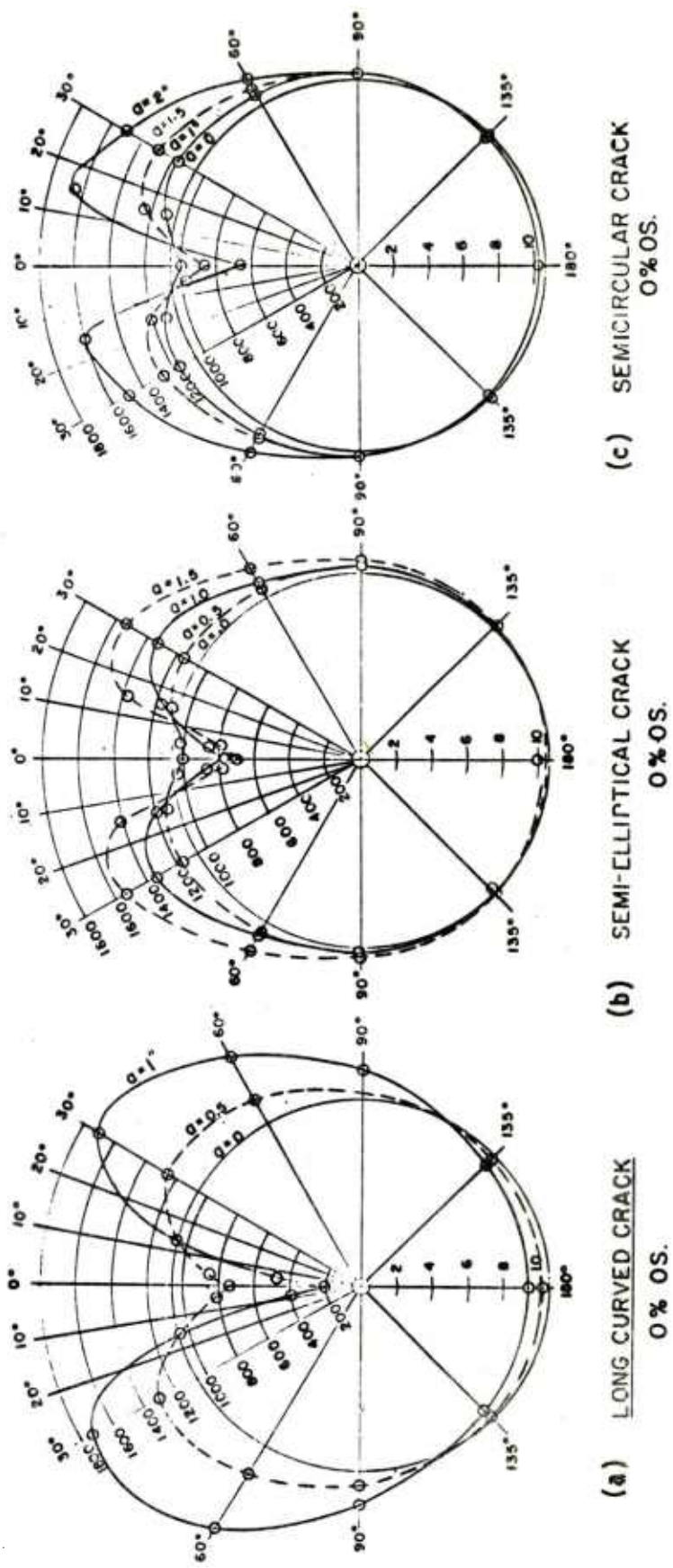
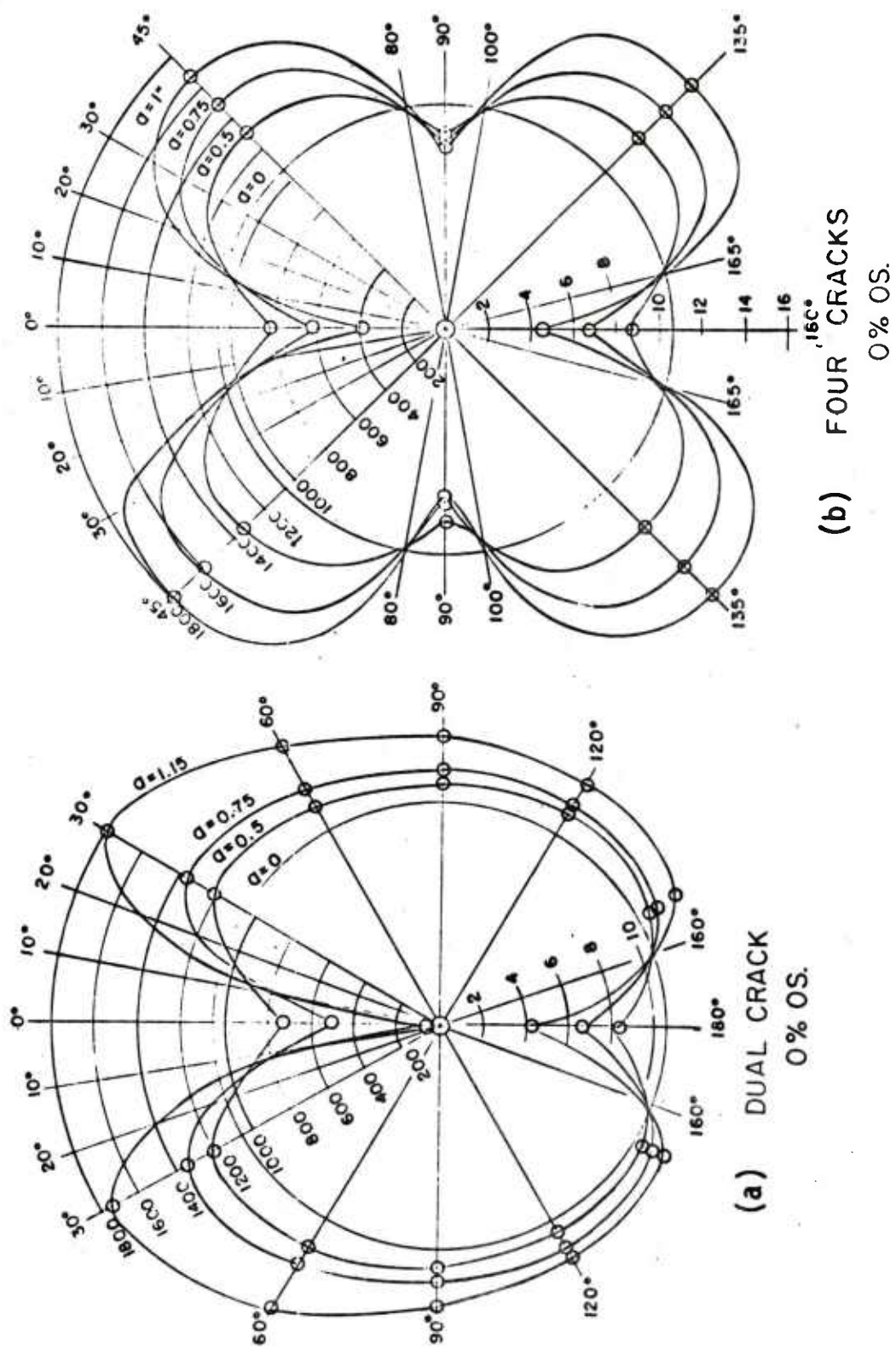


Fig. 2 POLAR PLOT OF STRAINS IS SIMILAR TO A CARDIOID.



It is found that the greatest decrease from the Lamé strain occurs directly over the crack, while the greatest increase above the Lamé strain occurs at approximately 15° on either side of the crack. At angles remote from the crack the strains remain approximately equal to the Lamé strain for the given pressure.

It is also found that as the crack deepens, the strain directly over the crack diminishes from the tensile Lamé strain expected in an uncracked cylinder and approaches zero strain in a regular manner with increasing crack depth. When this strain reaches zero or becomes compressive the fracture of the cylinder is imminent. During this time the pressure within the crack is exerting a bending moment on the remaining ligament as well as adding to the circumferential tension, and the compressive strain on the outside of the ligament becomes greater than the circumferential tensile strain. When the remaining ligament finally becomes thin enough the tension in it once again exceeds the bending strains and stretches the ligament to failure. In tough and ductile steel this may simply result in a small leak in the cylinder wall as the crack pierces it. Even this type of failure releases a large amount of strain energy, whereas a brittle fracture would result in fragmentation. In either case the decrease of tensile strain over the crack provides a warning preceding failure.

Figures 4 and 5 show that autofrettage by overstrain of the cylinders increases the crack tolerances. Figure 4, the polar plot for 30% overstressed cylinders, shows a greater crack tolerance than Figure 2, since at the cusp the decrease from the Lamé theoretical strain is less, for instance, at crack

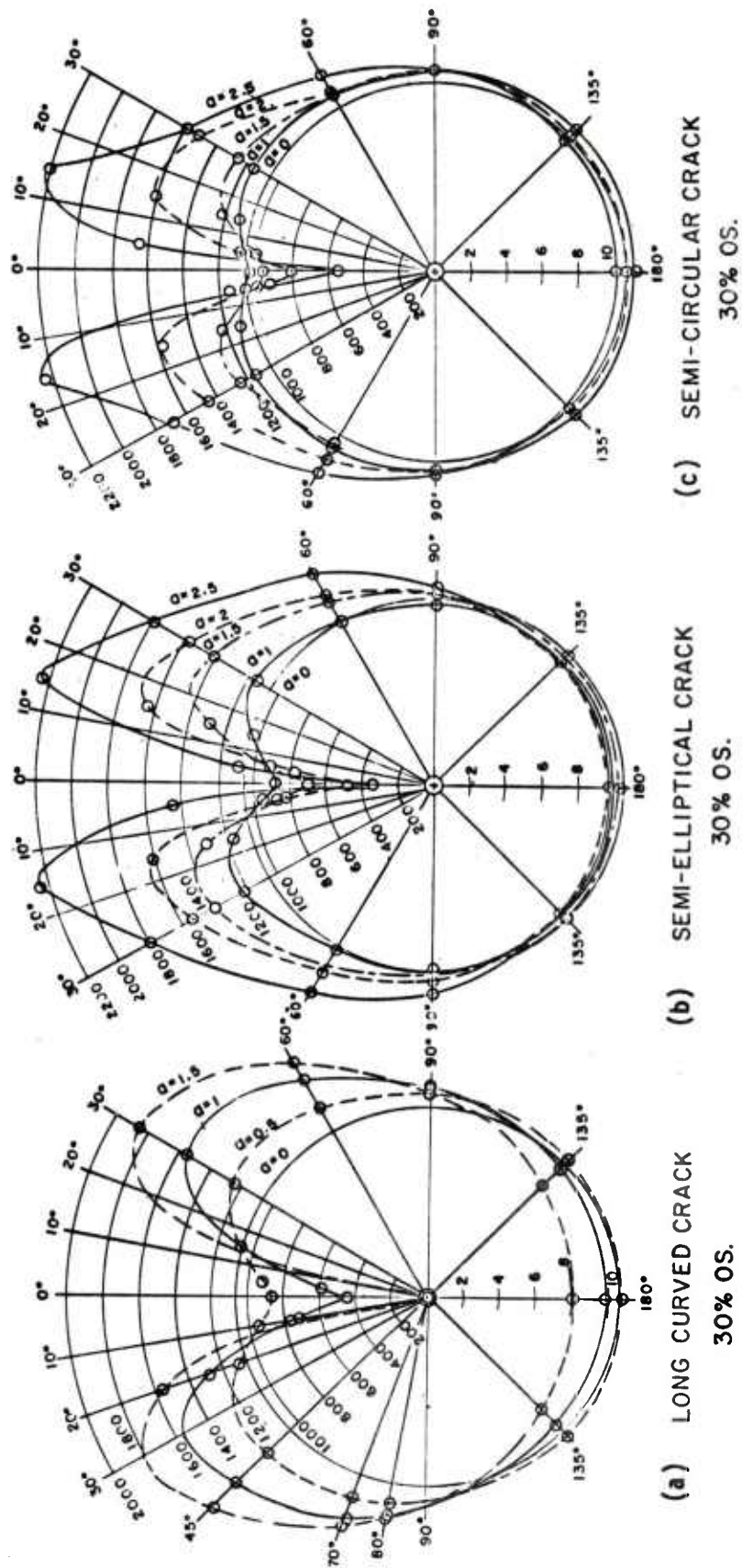


Fig. 4 POLAR PLOT FOR 30% OVERSTRAINED CYLINDERS SHOWS INCREASED CRACK TOLERANCE.

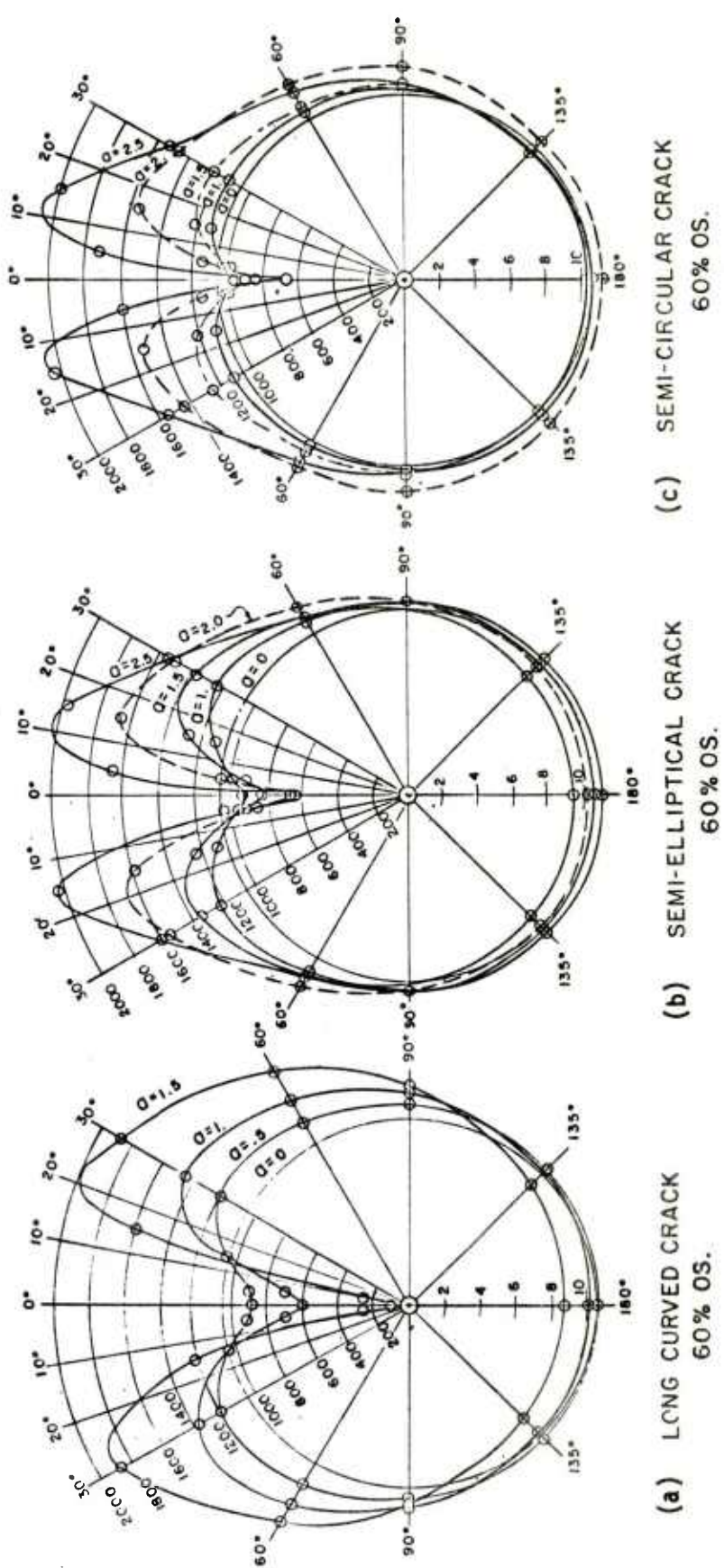


Fig. 5 POLAR PLOT FOR 60% OVERSTAINED CYLINDERS SHOWS STILL GREATER CRACK TOLERANCE.

depth $a = 1$ inch, than that of the corresponding non-autofrettaged cylinder. Figure 5, the polar plot for 60% overstrained cylinders, shows still greater crack tolerance. The cusps are shallower and the peak strains are closer to the crack plane, indicating increased resistance to the crack opening.

Figure 6 shows crack depth plotted versus number of fatigue loadings for 0%, 30%, and 60% overstrained cylinders with long curved cracks, semi-elliptical cracks and semicircular cracks. It is noted that the fatigue life increases with percent overstrain and also with aspect ratio $a/2c$ of the crack, going from $a/2c = .012$ for the long curved crack to $a/2c = .250$ for the semi-elliptical crack and to $a/2c = .500$ for the semicircular crack.

Figure 7 indicates strain measured at the crack plane, $\phi = 0^\circ$, plotted versus number of fatigue loadings for 0%, 30%, and 60% overstrained cylinders with long curved cracks, semi-elliptical cracks, and semicircular cracks. In all cases the strain diminishes to zero and becomes compressive (negative) as failure is approached, and suddenly goes tensile at failure. This terminal phenomenon indicates that the bending effect measured by the external strains is overcome by the tensile effect as the remaining ligament becomes smaller and cannot support the bending moment any longer.

Figure 8 shows the strain ratio, ϵ_o/ϵ_{th} , of the crack-plane strain to the theoretical strain plotted versus " a ", the crack depth. The dashed curves are calculated from Shannon's uniform wall thinning and pressure bending idealization for a straight-fronted crack in a non-autofrettaged cylinder, the crack depth for any strain for a curved front being a multiple of that for the straight front. Curves for 0%, 30%, and 60% overstrained cylinders are

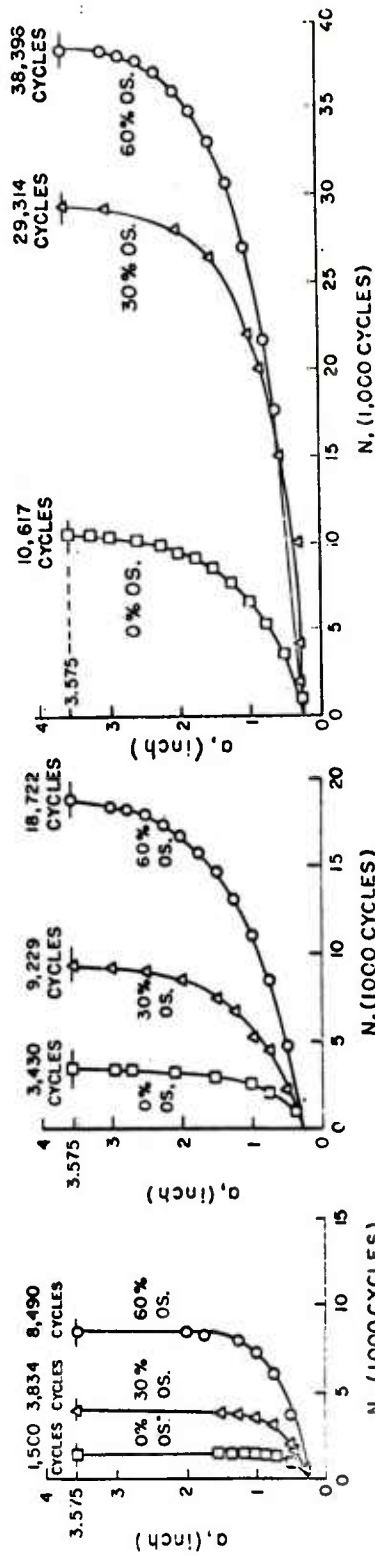


Fig. 6 CRACK DEPTH PLOTTED VERSUS NUMBER OF FATIGUE LOADINGS.

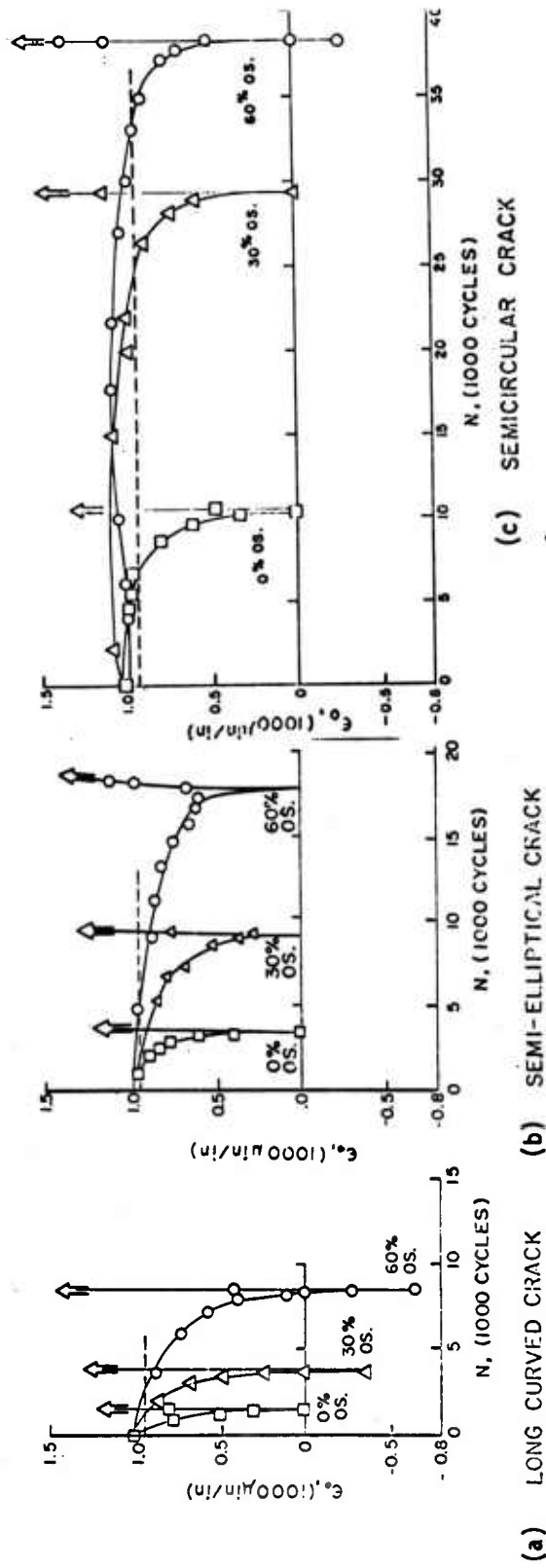


Fig. 7 STRAIN MEASURED AT CRACK PLANE, $\phi = 0$, PLOTTED VERSUS NUMBER OF FATIGUE LOADINGS.

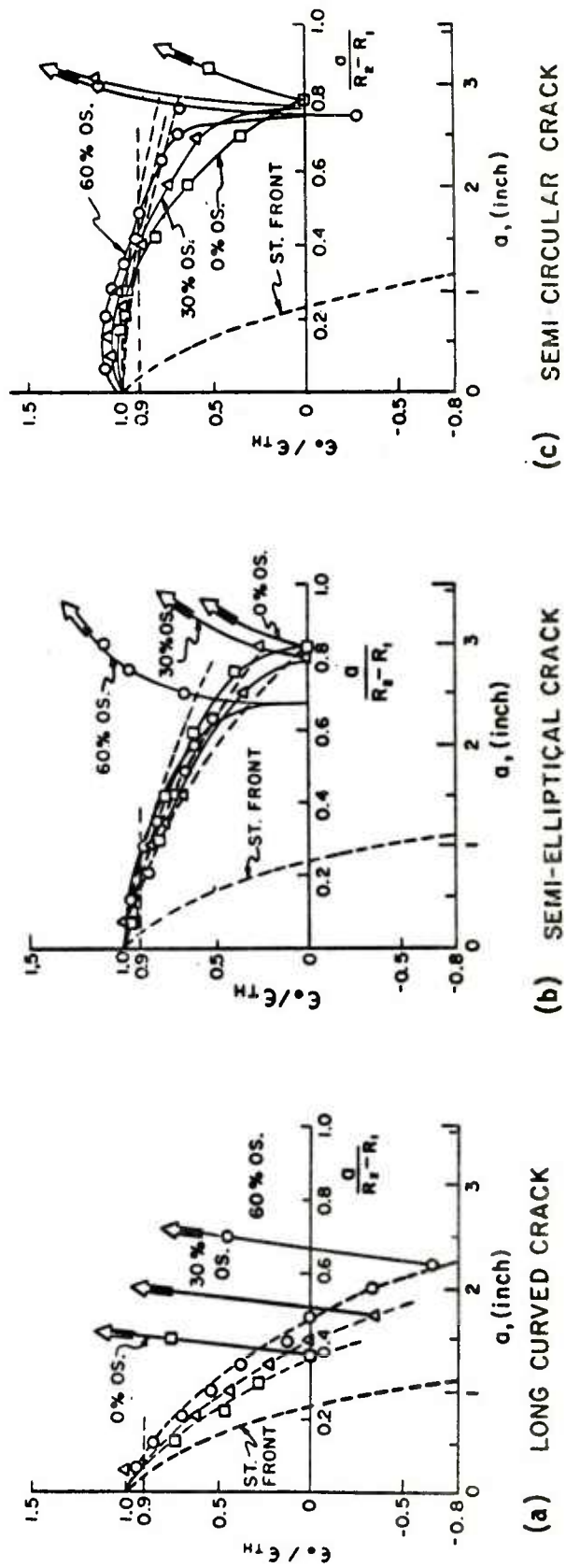


Fig. 8 STRAIN RATIO, ϵ_0/ϵ_{th} , OF THE ZERO-ANGLE STRAIN TO THE THEORETICAL STRAIN PLOTTED VERSUS CRACK DEPTH.

compared for long curved cracks, semi-elliptical cracks and semicircular cracks. The data is approximated by these calculated curves until a 10% reduction of ϵ_o/ϵ_{th} is exceeded, after which the measured values decrease more rapidly than the calculated curves as failure is approached.

Figure 9 shows σ_o/P for external stress calculated from Equation (6) and plotted versus crack depth. This graph shows that Equation (6) represents a decreasing stress, and hence Equation (7) represents a decreasing strain, at the OD as the crack depth is increased for a given value of pressure P . At some crack depth, therefore, the OD strain over the crack will have decreased from the theoretical Lamé' tensile value for that pressure (Eq. (1)), passed through zero and become compressive (negative), as shown at $a/(R_2-R_1)$ equal to about 0.25 in Figure 9. As indicated in Figure 8, failure of the test specimens occurred soon after the strain became compressive (negative), but at a greater crack depth than calculated for the straight-fronted crack.

Figure 9 also shows σ_I/P for internal stress at the crack tip calculated from Equation (8). This shows that Equation (8) starts at a stress given by Equation (3) for zero crack depth and increases with increasing crack depth for a given value of pressure P . In Figure 9 it gives a stress that becomes equal to the yield strength of 170 ksi (1172 MPa) for this particular material at approximately the depth where the OD strain becomes compressive in these specimens. Continued cyclic yielding at the crack tip leads to rapid fatigue failure from this crack depth because the remaining ligament can no longer support bending and behaves more like a thin wall cylinder in the crack zone as the remaining ligament gets thinner.

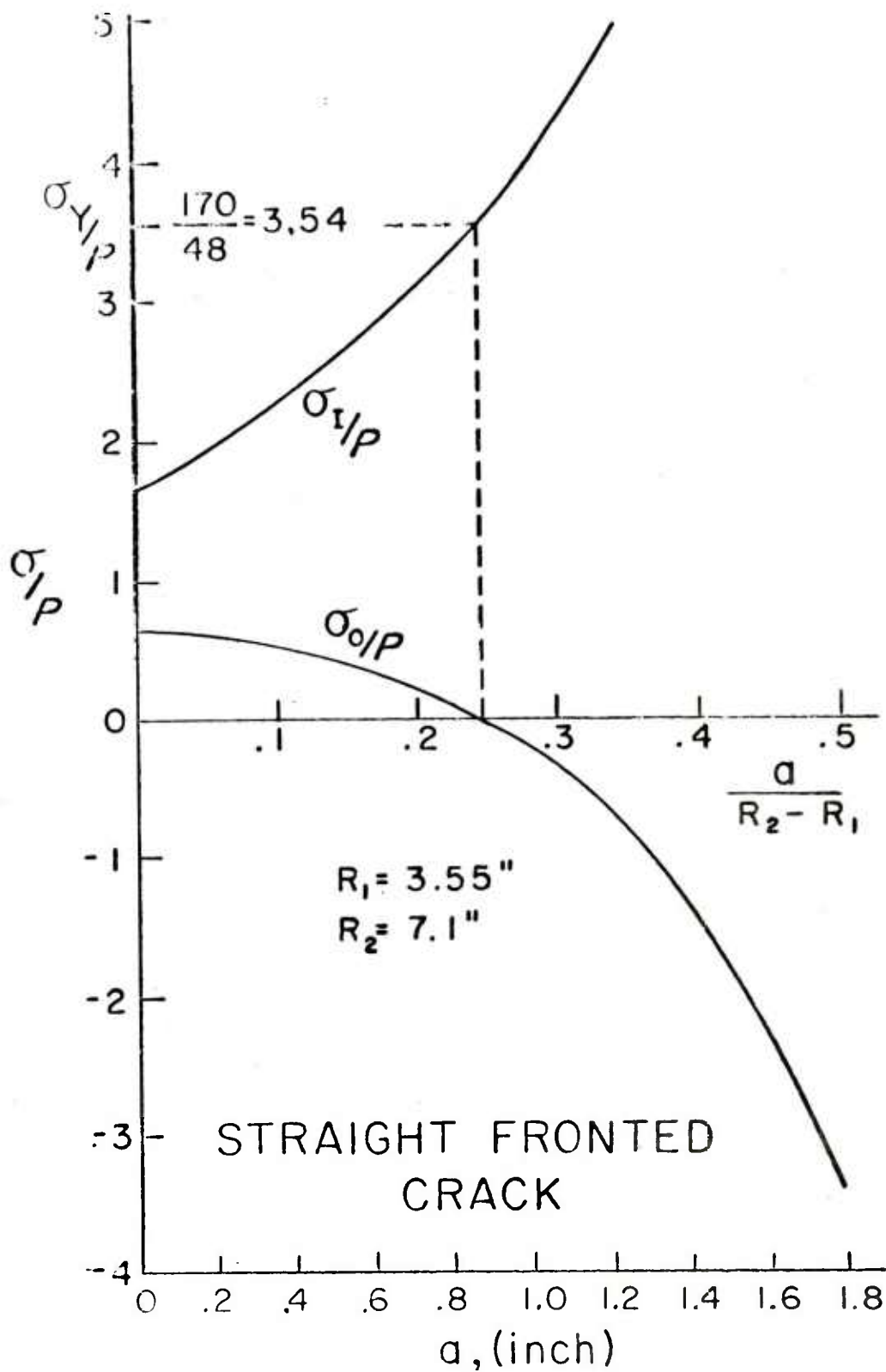


Fig. 9 PLOT OF CALCULATED σ_O/P FOR EXTERNAL STRESS AND σ_I/P FOR INTERNAL STRESS AT THE CRACK TIP.

Figure 10 shows a plot of strain ratio, ϵ_o/ϵ_{th} , versus fraction of fatigue life. The form of curve indicates that fraction of fatigue life is a function of the initial notch shape and relatively insensitive to the percent overstrain, even though percent overstrain enhances absolute fatigue life. The results for the long curved cracks (20 inch notch) fall in a band with the lower bound expressed by the ellipse. Those for the semi-elliptical cracks (4 inch notch) fall in a higher band and those for the semicircular cracks (1/2 inch notch) fall in the highest band. As indicated, the results for 0%, 30%, and 60% overstrained cylinders fall in the band for the given crack shape, indicating that the fraction of life expended is relatively insensitive to the percent overstrain. However, the higher the aspect ratio, $a/2c$, the greater the fraction of life, N/N_f , that will have been expended when ϵ_o has decreased to 90% of ϵ_{th} , as may be seen in Figure 10.

As an example of the possible use of Figure 10, consider a similar sized cylinder which has been subjected to 10,000 pressure cycles, and upon inspection is found to have a radial crack at the bore. If ultrasonic measurements show that the crack is 0.5 inch deep and 2 inches long, the aspect ratio is $a/2c = 0.25$, which corresponds to the middle band on Figure 10. If a circumferential strain gage mounted on the outside surface over the crack reads a strain that is 70% of the theoretical strain for the uncracked cylinder at the same pressure, the fraction of life N/N_f for $\epsilon_o/\epsilon_{th} = 0.7$ can be read from Figure 10. This gives a maximum $N/N_f = 0.9$, or $N_f = 11,100$ cycles, and a minimum $N/N_f = 0.8$, or $N_f = 12,500$ cycles. Thus failure is imminent and should be expected within the next 1,100 to 2,500 cycles if the pressure cycling is continued.

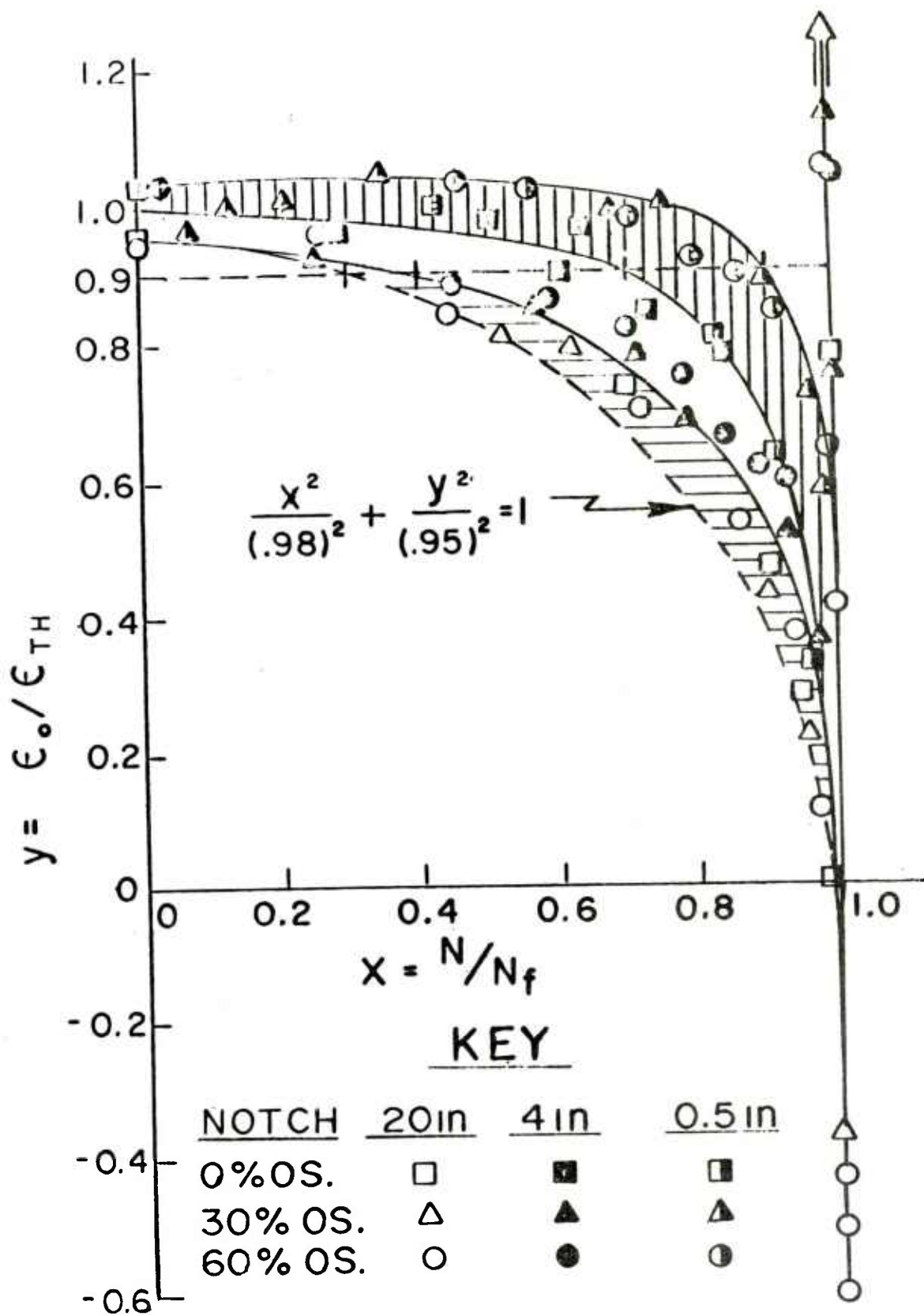


Fig. 10 STRAIN RATIO, ϵ_0/ϵ_{th} , VERSUS FRACTION OF FATIGUE LIFE, N/N_f .

It should be noted that a longer notch of smaller aspect ratio would have required a greater amount of autofrettage in order to endure 10,000 cycles for that depth, and its N/N_f would be smaller than that in the example. Conversely, a semicircular notch would have reached that depth at that number of cycles with less autofrettage and its N/N_f , in the upper band of Figure 10, would be greater.

CONCLUSIONS

(a) The fraction of fatigue life, N/N_f , that has been expended at any given crack depth is indicated by the strain ratio ϵ_o/ϵ_{th} for particular crack shapes. When ϵ_o diminishes to zero, failure is imminent. When ϵ_o has reduced to 90% of the theoretical Lamé' strain, a long curved crack has reached 30 to 40% of life, a semi-elliptical crack has reached 40 to 70% and a semicircular crack has reached 70 to 90% of the fatigue life.

(b) Measurement of the external circumferential strain over the dominant internal crack, along with the determination of the crack depth and shape by ultrasonic technique, enables one to estimate the fraction of fatigue life that has been expended in getting to that crack size.

(c) This procedure provides a practical means of estimating the fatigue life from fatigue tests of only a few cylinders.

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DIRECTOR US ARMY INDUSTRIAL BASE ENG ACT ATTN: DRXPE-MT ROCK ISLAND, IL 61201	1	MECHANICAL PROPERTIES DATA CTR BATTELLE COLUMBUS LAB 505 KING AVE COLUMBUS, OHIO 43201	1
CHIEF, MATERIALS BRANCH US ARMY R&S GROUP, EUR BOX 65, FPO N.Y. 09510	1	MATERIEL SYSTEMS ANALYSIS ACTV ATTN: DRXSY-MP ABERDEEN PROVING GROUND MARYLAND 21005	1
COMMANDER NAVAL SURFACE WEAPONS CEN ATTN: CHIEF, MAT SCIENCE DIV DAHLGREN, VA 22448	1		
DIRECTOR US NAVAL RESEARCH LAB ATTN: DIR, MECH DIV CODE 26-27 (DOC LIB) WASHINGTON, D. C. 20375	1 1		
NASA SCIENTIFIC & TECH INFO FAC P. O. BOX 8757, ATTN: ACQ BR BALTIMORE/WASHINGTON INTL AIRPORT MARYLAND 21240	1		

NOTE: PLEASE NOTIFY COMMANDER, ARRADCOM, ATTN: BENET WEAPONS LABORATORY, DRDAR-LCB-TL, WATERVLIET ARSENAL, WATERVLIET, N.Y. 12189, OF ANY REQUIRED CHANGES.